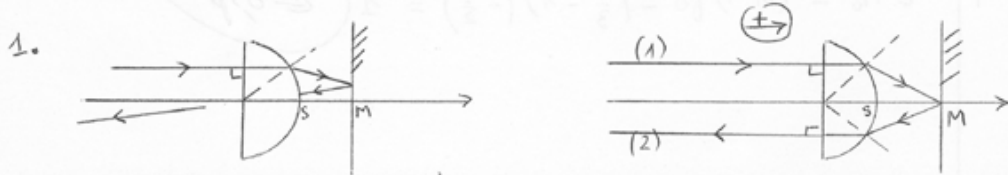


- I. 1. $i > i_0 = \text{Arc sin}(\frac{n_2}{n_1}) \approx 81,89^\circ$ réflexion totale.
 2. O.N. = $n_0 \sin \theta_0 = 1 \times \sin \theta_0 = n_1 \sin \alpha_0$ où $\alpha_0 = 90^\circ - 81,89 \approx 8,11^\circ$
 $O.N. = \sin \theta_0 \approx 0,204 \Rightarrow \theta_0 = 11,80^\circ \Rightarrow 2 \theta_0 = 23,6^\circ$
 3. $(AH)_{\text{mini}} = (AH)_0 = R_1 \tan i_0$; trajectoire du rayon = $AB = \frac{R_1}{\cos i_0}$
 $\frac{d_{\text{max}}}{d} = \frac{AB}{(AH)_m} = \frac{R_1}{\cos i_0} \cdot \frac{1}{R_1 \tan i_0} = \frac{1}{\sin i_0} = \frac{n_1}{n_2} = 1,01$

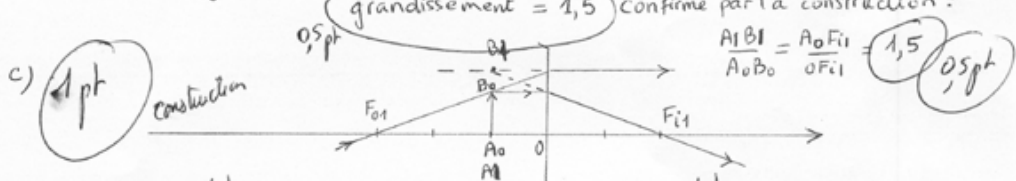
II.



1. $\frac{n_i}{P_i} - \frac{n_o}{P_o} = \frac{n_i - n_o}{R} \Rightarrow \left[\frac{1}{(P_i = SM)} - \frac{n}{(P_o = \infty)} = \frac{1-n}{-1} \right] \Leftrightarrow \frac{1}{z_1} = \frac{1}{1,8} = \frac{1-n}{-1} = n-1 = 0,555$
 $\Rightarrow n = 1,555$

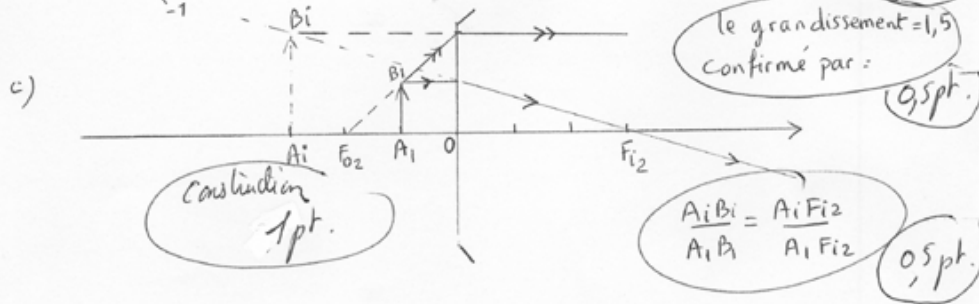
III. 1. a) $\beta_{01} = \overline{OF_{01}} = \frac{R_1 n_o}{n_o - n_i} = \frac{-1 \times 1,5}{1,5 - 1} = -3 \text{ cm}$; $\beta_{i1} = \frac{R_1 n_i}{n_i - n_o} = \frac{-1 \times 1}{-0,5} = 2 \text{ cm}$

b) $\frac{1}{(P_i)} - \frac{1,5}{(-1)} = \frac{n_i - n_o}{R_1} = \frac{1 - 1,5}{-1} = 0,5 \Rightarrow \frac{1}{P_i} = -1 \Rightarrow P_i = -1 = \overline{OA_1}$



2. a) $\beta_{02} = \overline{OF_{02}} = \frac{R_2 n_o}{n_o - n_i} = \frac{1 \times 1}{1 - 1,5} = -2 \text{ cm}$; $\beta_{i2} = \frac{R_2 n_i}{n_i - n_o} = \frac{1 \times 1,5}{0,5} = 3 \text{ cm}$

b) $\frac{1,5}{P_i} - \frac{1,5}{P_o} = \frac{1,5 - 1}{1} = 0,5 \Rightarrow \frac{1,5}{P_i} = -1 + 0,5 = -0,5 \Rightarrow P_i = -3 \text{ cm}$



3.

$$3. T(\vec{E}_S) = \underbrace{\begin{pmatrix} 1 & 1/3/2 \\ 0 & 1 \end{pmatrix}}_{\text{translation } 0.5} \underbrace{\begin{pmatrix} 1 & 0 \\ -0.5 & 1 \end{pmatrix}}_{\text{D2 refractions}} \underbrace{\begin{pmatrix} 1 & 0 \\ -0.5 & 1 \end{pmatrix}}_{\text{D1}} \underbrace{\begin{pmatrix} 1 & 1/3/2 \\ 0 & 1 \end{pmatrix}}_{\text{translation } E_0} = \begin{pmatrix} 1/3 & 0 \\ -1 & 1/3 \end{pmatrix}$$

4

$$V = 1; \quad f_0 = -\frac{n_0}{V} = -1,5 \quad ; \quad f_i = \frac{n_i}{V} = 1,5$$

$$\overline{S}H_i = (a-1) f_i = \left(\frac{1}{3} - 1\right) \cdot \frac{3}{2} = -1 \quad \leftarrow 0,5 \text{ pt.}$$

$$\overline{E}H_0 = (d-1) f_0 = \left(\frac{1}{3} - 1\right) \left(-\frac{3}{2}\right) = 1 \quad \leftarrow 0,5 \text{ pt.}$$

Total \equiv 22 points.